

VEHICLE ROUTING IN BEVERAGE INDUSTRY

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VEHICLE ROUTING IN BEVERAGE INDUSTRY

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ABSTRACT

A classical problem in distribution logistics is the problem of designing least cost routes from one depot to a set of geographically scattered points. All routes start and end at the depot, and the total demands of all points on one particular route must not exceed the capacity of the vehicle. This problem is known as the Vehicle Routing Problem (VRP). If each customer to be served is associated with two quantities of goods to be collected and delivered, the problem is then called the Vehicle Routing Problem with Pick-up and Delivery (VRPPD). In this paper, the Vehicle Routing Problem with Pick-up and Delivery (VRPPD) is used to solve the distribution problem face by a beverage industry where vehicles of a certain loading capacity must routinely visit several retailers. Each retailer has a certain demand of full bottles to be delivered and empty bottles to be picked-up and be brought back to the depot. A heuristic algorithm is then used to construct the routes with the objective of minimizing not only the number of vehicles required, but also the total travel distance (or total cost) incurred by the fleet of vehicles.

Keywords: Vehicle Routing Problem, Pick-up and Delivery, Heuristic

1. INTRODUCTION

In the classical vehicle routing problem, goods are delivered from a depot to a set of customers using a set of identical delivery vehicles. Each customer demands a certain quantity of goods and the delivery vehicles have a limited capacity. Typically, the problem objective is to find delivery routes starting and ending at the depot that minimize a total travel distance (or cost) without violating the capacity constraints of the vehicles. In some VRPs, the problem objective might be to determine the minimum number of delivery vehicles to serve all customers.

In the distribution system of a beverage industry, the delivery of full bottles from the depot to the customers has to be performed simultaneously with the pick-up of collected empty bottles to be brought back to the depot. The problem is then called the vehicle routing problem with pick-up and delivery (VRPPD), which is a variant of the classical VRP.

One important characteristic of VRPPD is that a vehicle's load in any given route is a mix of delivery and pick-up loads, at the same time. In any route the vehicle can not violate some constraints, such as the vehicle capacity and traveling distance constraints. In a traditional VRP setting, this can lead to bad utilization of

the vehicles capacities, increase travel cost (distances), or a need for more vehicles.

The VRPSDP was first introduced by Min (1989). He presented a cluster-first-route-second algorithm to solve a problem of transporting books between libraries by two vehicles. Dethloff (2001) developed insertion-based heuristics that use four different criteria to solve the problem. Gribkovskaia, Halskau and Myklebost (2001) developed a so-called *Lasso Solutions* that allows some customers to be visited twice by the same vehicle. Tang and Galvao developed a local search heuristics (2002) and a tabu search algorithm (2006). Angelelli and Mansini (2002) using a branch-and-price algorithm which is an exact algorithm originally developed for the classical VRP.

The aim of this paper is to propose a load-based insertion procedure that extends the idea of the 1-insertion heuristic of Solomon (1987). The rest of this paper is organized as follows: In section 2 a problem formulation of VRPPD is discussed. Section 3 is devoted to a discussion of the developed heuristic to solve VRPPD. Section 4 gives a numerical example for the proposed heuristic. The conclusion is put in section 5.

2. PROBLEM FORMULATION

The VRPPD is defined on a graph (N, A) . The node set N consists of the set of customers, denoted by C , and the node 0 which represent the depot. The number of customers $|C|$ will be denoted n and the customers will be denoted by $1, 2, \dots, n$. The arc set A corresponds to possible connections between the nodes. All routes start and end at node 0. The set of (identical) vehicles is denoted by V . Each vehicle has a given capacity Q and is based at the depot. Each customer i has a pickup demand p_i and a delivery demand d_i satisfying $p_i \geq 0, d_i \geq 0, \sum_{i=1}^n p_i \leq Q$ and $\sum_{i=1}^n d_i \leq Q$. Each arc $(i, j) \in A$ of the network is associated with a cost C_{ij} .

The mathematical model, which is adapted from the general assignment model of Fisher and Jaikumar (1981), contains a decision variable X_{ijk} ($\forall (i, j) \in A, \forall k \in V$) which is equal to 1 if vehicle k drives from node i to node j , and 0 otherwise. The objective is to construct a set of least cost routes, one for each vehicle, starting and ending at the depot, and making all pickups and deliveries without ever exceeding the vehicle capacity. It is assumed that transshipments are not allowed, and pick-up and delivery demands are unsplitable.

The VRPPD can be stated mathematically as:

$$\text{Min} \sum_{k \in V} \sum_{(i, j) \in A} C_{ij} X_{ijk} \quad (1)$$

Subject to:

$$\sum_{k \in V} \sum_{j \in N} X_{ijk} = 1 \quad \forall i \in C \quad (2)$$

$$\sum_{i \in C} d_i \sum_{j \in N} X_{ijk} \leq Q \quad \forall k \in V \quad (3)$$

$$\sum_{i \in C} p_i \sum_{j \in N} X_{ijk} \leq Q \quad \forall k \in V \quad (4)$$

$$X_{ijk} \in \{0, 1\} \quad \forall (i, j) \in A, \forall k \in V \quad (5)$$

The objective function (1) states that costs should be minimized. Constraint set (2) states that each customer must be assigned to exactly one vehicle. Constraint set (3) and (4) states that no vehicle can service more customers than its capacity permits, while (5) is the set of integrality constraints.

The above formulation is very universal, and can easily turn into other classical vehicle routing problems. If $p_i = 0$, then it becomes a conventional VRP. If all customers only have delivery or pick-up demands (either p_i or d_i equals 0), then it changes into VRPPD equivalent; if only one vehicle can finish service, then it turns into TSP equivalent.

3. HEURISTIC FOR VRPPD

Since the VRP is an NP-hard combinatorial optimization problem, the exact algorithms can only solve relatively small problems. Therefore, in this section a relatively simple heuristic algorithm, called the insertion procedures, is developed to obtain a quick solutions for a large problems.

Feasibility Condition

The delivery or pick-up-feasibility condition are necessary and sufficient conditions for route feasibility in a pure VRP setting. We can see that the delivery or pick-up feasibility of the route depends only on the set of customers assigned to the vehicle such that the total delivery (or pick-up) of the route does not exceed the vehicle's capacity. It will not depend on the sequence the customers are visited in.

In the VRPPD, the vehicle's capacity can be violated at any node of the route. Such a violation will depend on the sequence of the customers. Let $C_p(i), C_d(i)$ and $L(i)$ be the cumulative pick-up, the cumulative delivery, and the vehicle load at node i of the route R . Notice that the vehicle load at any point of the route R in the VRPPD is a function of the cumulative pick-up, the cumulative delivery, and the initial load value, i.e.,

$$L(i) = L(0) + C_p(i) - C_d(i); i \in R$$

Therefore, even when each of the cumulative demands $C_p(i)$ and $C_d(i)$ at any node i of the route do not exceed the vehicle's capacity, the vehicle's load $L(i)$ can exceed the vehicle's capacity. This means that the route becomes infeasible. Thus in the VRPPD, all the three types of feasibility must be obeyed. That is, a

9 route is feasible if and only if it is delivery-feasible, pick-up-feasible, and load-feasible.

Route Construction

There have been several attempts to develop heuristics for the VRPPD. These are usually modifications of well-known procedures for the basic VRP such as the saving heuristics, insertion procedures, space filling curves, tour-partitioning procedures, and many others. In this paper a load-based insertion procedure is proposed as the extension to the idea of the 1-insertion heuristic of Solomon (1987).

1 The concept of the insertion procedures is to successively insert customers into growing routes. In this proposed heuristic, a route is first initialized with a seed customer (node). The remaining unrouted nodes are added 17 this route until it is full with respect to the capacity constraint. If unrouted nodes remain, the procedures of initializations and insertion are then repeated until all customers are serviced. The seed nodes are selected by finding either the unrouted node with large pick-up demands or with large difference between pick-up and delivery demands. The detail of the procedures is as follows.

Step 0:
Calculate the minimum number of vehicles needed to serve all customers, i.e.

$$V = \max \left\lceil \frac{\sum_{i \in C} d_i}{Q} \right\rceil, \left\lceil \frac{\sum_{i \in C} p_i}{Q} \right\rceil$$

Go to step 1

Step 1:
Choose a set of seed nodes $i_s, s=1, \dots, V$, each one assigned to one vehicle. Define the rest of the nodes as the free nodes. Go to step 2.

Step 2:
Take a seed node not used so far. Initialize a partial route with the chosen seed node in it, starting from and end at the depot. Go to step 3.

Step 3:
Let $(0, i_1, \dots, 0)$ be the current partial route. For each of the unrouted free node u , calculate the additional cost of inserting u to the partial route as $Z_1(i, u, j) = C_{iu} + C_{uj} - C_{ij}$. Next calculate $Z_2(i, u, j) = C_{0u} - Z_1(i, u, j)$ where

C_{0u} is the cost of reaching node u straight from the depot. Go to step 4.

Step 4:
Insert node u with minimum $Z_1(i, u, j)$ between adjacent node i and j in the current partial route. Call this new route R . Go to step 5.

Step 5:
Calculate $C_d(R) = \sum_{i \in R} d_i$ and set $L(0) = C_d(R)$.
Calculate $L(i) = L(0) + C_p(i) - C_d(i); i \in R$
If $L(i)$ does not exceed the vehicle's capacity, go to step 6. Otherwise, go to step 7

Step 6:
Do the next insertion of the unrouted free node u with minimum $Z_2(i, u, j)$ between the adjacent node i and j in the current partial route. Call this new route R . Back to step 5.

Step 7:
Drop the last inserted node from the route and define the final feasible route of the vehicle. If any seed nodes remain, back to step 2. Otherwise, stop.

4. NUMERICAL EXAMPLE

Suppose we have a graph that consists of a depot of softdrink industry and 12 customer points to serve. The cost matrix for the graph is given in Table 1, while the delivery and pick-up demands are given in Table 2. It is assumed that there is a homogeneous fleet of vehicles with capacities equal to 35 units. Since the total delivery demands is 84 and the total pick-up demands is 94, we need at least 3 vehicles to serve all customers.

With respect to the difference between pick-up and delivery demands, node 9, 1, and 3 are chosen as the seed nodes, while the rest are defined as the free nodes. Let node 9 be the first seed chosen to build the route, so that the initial partial route 18 $R=(0, 9, 0)$. From the calculation of $Z_1(i, u, j)$ and $Z_2(i, u, j)$ given in Table 3, it is obvious that node 8 is the one to be inserted to the current partial route, since it has the minimum value of $Z_1(i, u, j)$. The new partial route is then $R=(0, 9, 8, 0)$, with $L(0) = C_d(R) = 13$; $L(9) = 17$; and $L(8) = 19$.

Since the load of the route is less than the vehicle's capacity, insert node 12, which has

the maximum value of $Z_2(i,u,j)$, to the current partial route. We now have $R=(0, 9, 8, 12, 0)$ with $L(0) = C_\alpha(R) = 22$; $L(9) = 26$; $L(8) = 28$; and $L(12) = 27$. The next free node to be inserted is node 10 so that we have $R=(0, 9, 8, 12, 10, 0)$ with $L(0) = C_\alpha(R) = 29$; $L(9) = 33$; $L(8) = 35$; $L(12) = 34$, and $L(10) = 34$.

Next, insert node 4 to the current partial route, so that we have $R=(0, 9, 8, 12, 10, 4, 0)$ with $L(0)=C_\alpha(R)=37$ which is exceeding the vehicle's capacity. Hence, drop node 4 from the route. The feasible route of the first vehicle is then $R=(0, 9, 8, 12, 10, 0)$ with the associated travel cost of 31.7.

In a similar way as for the first vehicle, we now have Table 4 for the second vehicle that gives the feasible vehicle's route of $R=(0, 1, 4, 2, 5, 0)$. The associated travel cost of the second route is 23.9. Finally, we have Table 5 for the third vehicle. There are two feasible vehicle's routes, i.e. $R=(0, 3, 7, 6, 11, 0)$ with the associated travel cost of 25.4 and $R=(0, 3, 6, 7, 11, 0)$ with the associated travel cost of 26.1. We then choose the first alternative route to be the route of the third vehicle. Therefore, the total travel cost incurred by the fleet of the three vehicles is then 81.

Table 1. The Cost Matrix

Node	0	1	2	3	4	5	6	7	8	9	10	11
0	0	9.8	10.1	9.8	9.9	8.9	7.6	8.1	9.8	13.4	10.1	7.8
1	9.8	0	4.6	6	0.9	5.3	9.1	9.5	3.9	4.3	4.3	9.2
2	10.1	4.6	0	2.2	3.6	0.7	7	6.5	1.4	4.9	1.9	7.9
3	9.8	6	2.2	0	4.9	1.4	7	6.5	2.9	7.5	3.8	7.7
4	9.9	0.9	3.6	4.9	0	5.3	9.1	9.5	3.9	3.7	4.3	9.2
5	8.9	5.3	0.7	1.4	5.3	0	5.8	5.4	2.6	6.1	3.1	6.7
6	7.6	9.1	7	7	9.1	5.8	0	0.6	7	10.5	7.5	0.7
7	8.1	9.5	6.5	6.5	9.5	5.4	0.6	0	7.5	11.08	8	0.9
8	9.8	3.9	1.4	2.9	3.9	2.6	7	7.5	0	3.5	0.5	9.3
9	13.4	4.3	4.9	7.5	3.7	6.1	10.5	11.08	3.5	0	3.3	11.5
10	10.1	4.3	1.9	3.8	4.3	3.1	7.5	8	0.5	3.3	0	9.7
11	7.8	9.2	7.9	7.7	9.2	6.7	0.7	0.9	9.3	11.5	9.7	0

Table 2. The Delivery and Pick-up Demands

Demand	Node											
	1	2	3	4	5	6	7	8	9	10	11	12
Delivery	7	8	6	8	6	7	8	7	6	7	5	9
Pick-up	10	9	9	7	5	5	8	9	10	7	7	8

Table 3. The Value of $Z_1(i,u,j)$ and $Z_2(i,u,j)$ for Vehicle-1

i	u	d(i,u)	d(u,0)	d(i,0)	Z1(i,u,j)	Z2(i,u,j)
9	2	4.9	10.1	13.4	1.6	8.5
	4	3.7	9.9	13.4	0.2	9.7
	5	6.1	8.9	13.4	1.6	7.3
	6	10.5	7.6	13.4	4.7	2.9
	7	11.08	8.1	13.4	5.78	2.32
	8	3.5	9.8	13.4	-0.1	9.9
	10	3.3	10.1	13.4	0	10.1
	11	11.5	7.8	13.4	5.9	1.9
	12	3.1	10.9	13.4	0.6	10.3

Table 4. The Value of $Z_1(i,u,j)$ and $Z_2(i,u,j)$ for Vehicle-2

i	u	d(i,u)	d(u,0)	d(i,0)	Z1(i,u,j)	Z2(i,u,j)
1	2	4.6	10.1	9.8	4.9	5.2
	4	0.9	9.9	9.8	1	8.9
	5	5.3	8.9	9.8	4.4	4.5
	6	9.1	7.6	9.8	6.9	0.7
	7	9.5	8.1	9.8	7.8	0.3
	11	9.2	7.8	9.8	7.2	0.6

Table 5. The Value of $Z_1(i,u,j)$ and $Z_2(i,u,j)$ for Vehicle-3

i	u	d(i,u)	d(u,0)	d(i,0)	Z1(i,u,j)	Z2(i,u,j)
3	6	7	7.6	9.8	4.8	2.8
	7	6.5	8.1	9.8	4.8	3.3
	11	7.7	7.8	9.8	5.7	2.1

5. CONCLUSION

This paper has dealt with the vehicle routing problem that is frequently encountered in the distribution system of beverage industry, where the delivery of full bottles from the depot and the pick-up of empty bottles from the customers are performed simultaneously. Each customer can only be visited once by a vehicle without ever exceeding the vehicle capacity. To find the optimal solution of the problem, an integer programming model was developed based on the general assignment model of Fisher and Jaikumar. Since the optimization model can only solve relatively small problems, a heuristic algorithm, called the insertion procedures was also developed to solve the model more efficiently.

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